Fitness Evaluation and Selection

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Encoding

- Pitness Evaluation and Selection
- Mating pool
- Crossover
- Mutation
- Inversion
- Onvergence test

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Encoding

Pitness evaluation and Selection

- Mating pool
- Crossover
- Mutation
- Inversion
- Convergence test

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- After deciding an encoding scheme, the second important things is how to perform selection from a set of population, that is, how to choose the individuals in the population that will create offspring for the next generation and how many offspring each will create.
- The purpose of selection is, of course, to emphasize **fittest** individuals in the population in hopes that their offspring will in turn have even higher fitness.

Selection is the process for creating the population for next generation from the current generation

To generate new population: Breeding in GA

- Create a mating pool
- Select a pair
- Reproduce

• In GA, there is a need to create next generation

- The next generation should be such that it is toward the (global) optimum solution
- Random population generation may not be a wiser strategy
- Better strategy follows the biological process: Selection

Selection involves:

- Survival of the fittest
- Struggle for the existence

• Fitness evaluation is to evaluate the survivability of each individual in the current population

How to evaluate the fitness of an individual?

- A simplest strategy could be to take the confidence of the value(s) of the objective function(s)
 - Simple, if there is a single objective function
 - But, needs a different treatment if there are two or more objective functions
 - They may be in different scales
 - All of them may not be same significant level in the fitness calculation
 - . . . etc.



P1:	CBADFE	11
P2:	ABDCEF	19
P3:	ACBFED	16
P4:	FCDBEA	12
P5:	CFDABE	10

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Different strategies are known for the selection:

- Canonical selection (also called proportionate-based selection)
- Roulette Wheel selection (also called proportionate-based selection)
- Rank-based selection (also called as ordinal-based selection)
- Tournament selection
- Steady-state selection
- Boltzman selection

In this techniques, fitness is defined for the *i* – *th* individual as follows.

fitness
$$(i) = rac{f_i}{\overline{F}}$$

where f_i is the evaluation associated with the i - th individual in the population.

• \overline{F} is the average evaluation of all individuals in the population size *N* and is defined as follows.

$$\bar{F} = rac{\sum_{i=1}^{N} f_i}{N}$$

- In an iteration, we calculate $\frac{f_i}{F}$ for all individuals in the current population.
- In Canonical selection, the probability that individuals in the current population are copied and placed in the mating pool is proportional to their fitness.

Note :

- Here, the size of the mating pool is $p\% \times N$, for some *p*.
- Convergence rate depends on *p*.

Roulette-Wheel selection

- In this scheme, the probability for an individual being selected in the mating pool is considered to be proportional to its fitness.
- It is implemented with the help of a wheel as shown.



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Roulette-Wheel selection mechanism

- The top surface area of the wheel is divided into N parts in proportion to the fitness values $f_1, f_2, f_3 \cdots f_N$.
- The wheel is rotated in a particular direction (either clockwise or anticlockwise) and a fixed pointer is used to indicate the winning area, when it stops rotation.
- A particular sub-area representing a GA-Solution is selected to be winner probabilistically and the probability that the *i* – *th* area will be declared as

$$p_i = rac{f_i}{\sum_{i=1}^N f_i}$$

 In other words, the individual having higher fitness value is likely to be selected more.

The wheel is rotated for N_p times (where $N_p = p\% N$, for some p) and each time, only one area is identified by the pointer to be the winner.

Note :

- Here, an individual may be selected more than once.
- Convergence rate is fast.

Roulette-Wheel selection mechanism: An Example

Individual	Fitness value	pi
1	1.01	0.05
2	2.11	0.09
3	3.11	0.13
4	4.01	0.17
5	4.66	0.20
6	1.91	0.08
7	1.93	0.08
8	4.51	0.20



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Roulette-Wheel selection : Implementation

Input: A Population of size N with their fitness values **Output:** A mating pool of size N_p

Steps:

D Compute
$$p_i = \frac{f_i}{\sum_{i=1}^N f_i}, \forall i = 1, 2 \cdots N$$

- Calculate the cumulative probability for each of the individual starting from the top of the list, that is $P_i = \sum_{j=1}^{i} p_j$, for all $j = 1, 2 \cdots N$
- Generate a random number say r between 0 and 1.
- Select the j-th individual such that $P_{j-1} < r \le P_j$
- Sepeat Step 3-4 to select N_p individuals.



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Roulette-Wheel selection: Example

The probability that i-th individual will be pointed is

$$p_i = rac{f_i}{\sum_{i=1}^N f_i}$$

Example:

Individual	pi	Pi	r	Т
1	0.05	0.05	0.26	I
2	0.09	0.14	0.04	I.
3	0.13	0.27	0.48	П
4	0.17	0.44	0.43	I
5	0.20	0.64	0.09	П
6	0.08	0.72	0.30	
7	0.08	0.80	0.61	
8	0.20	1.0	0.89	I
B 1				
p _i = Probability of an individual		r = Ran	dom Number t	between 01

P_i = Cumulative Probability

T=Tally count of selection

Following are the point to be noted:

- The bottom-most individual in the population has a cumulative probability $P_N = 1$
- ② Cumulative probability of any individual lies between 0 and 1
- The i-th individual in the population represents the cumulative probability from P_{i-1} to P_i
- The top-most individual represents the cumulative probability values between 0 and p_1
- S It may be checked that the selection is consistent with the expected count $E_i = N \times p_i$ for the *i*-th individual.

Does the selection is sensitive to ordering, say in ascending order of their fitness values?

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- Suppose, there are only four binary string in a population, whose fitness values are *f*₁, *f*₂, *f*₃ and *f*₄.
- Their values 80%, 10%, 6% and 4%, respectively.

What is the expected count of selecting f_3 , f_4 , f_2 or f_1 ?

Problem with Roulette-Wheel selection scheme

The limitations in the Roulette-Wheel selection scheme can be better illustrated with the following figure.



The observation is that the individual with higher fitness values will guard the other to be selected for mating. This leads to a lesser diversity and hence fewer scope toward exploring the alternative solution and also premature convergence or early convergence with local optimal solution.

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Rank-based selection

- To overcome the problem with Roulette-Wheel selection, a rank-based selection scheme has been proposed.
- The process of ranking selection consists of two steps.
 - Individuals are arranged in an ascending order of their fitness values. The individual, which has the lowest value of fitness is assigned rank 1, and other individuals are ranked accordingly.
 - The proportionate based selection scheme is then followed based on the assigned rank.

Note:

• The % area to be occupied by a particular individual *i*, is given by

$$\frac{r_i}{\sum_{i=1}^N r_i} \times 100$$

where r_i indicates the rank of i - th individual.

• Two or more individuals with the same fitness values should have the same rank.

Rank-based selection: Example

- Continuing with the population of 4 individuals with fitness values: $f_1 = 0.40, f_2 = 0.05, f_3 = 0.03$ and $f_4 = 0.02$.
- Their proportionate area on the wheel are: 80%, 10%, 6% and 4%
- Their ranks are shown in the following figure.

Individual	Fitness	RW	Rank	RS
(i)	(fi)	(Area)		(Area)
1	0.4	80 %	4	40 %
2	0.05	10 %	3	30 %
3	0.03	6 %	2	20 %
4	0.02	4 %	1	10 %



It is evident that expectation counts have been improved compared to Routlette-Wheel selection.

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Rank-based selection: Implementation

Input: A population of size N with their fitness values **Output:** A mating pool of size N_p .

Steps:

- Arrange all individuals in ascending order of their fitness value.
- Rank the individuals according to their position in the order, that is, the worst will have rank 1, the next rank 2 and best will have rank N.
- Apply the Roulette-Wheel selection but based on their assigned ranks. For example, the probability p_i of the i-th individual would be

$$p_i = \frac{r_i}{\sum_{j=1}^i r_j}$$

Stop

Comparing Rank-based selection with Roulette-Wheel selection

_					
l	Individual	% Area	fi	Rank (r _i)	% Area
	1	80 %	0.4	4	40 %
	2	10 %	0.05	3	30 %
	3	7 %	0.03	2	20 %
	4	4 %	0.02	1	10 %
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A rank-based selection is expected to performs better than the Roulette-Wheel selection, in general.

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Basic concept of tournament selection

Who will win the match in this tournament?



- In this scheme, we select the tournament size n (say 2 or 3) at random.
- We pick *n* individuals from the population, at random and determine the best one in terms of their fitness values.
- The best individual is copied into the mating pool.
- Thus, in this scheme only one individual is selected per tournament and N_p tournaments are to be played to make the size of mating pool equals to N_p.

Note :

- Here, there is a chance for a good individual to be copied into the mating pool more than once.
- This techniques founds to be computationally more faster than both Roulette-Wheel and Rank-based selection scheme.

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The tournament selection scheme can be stated as follows.

Input : A Population of size N with their fitness values **Output** : A mating pool of size $N_p(N_p \le N)$

Steps:

- Select N_U individuals at random $(N_U \le N)$.
- ② Out of N_U individuals, choose the individual with highest fitness value as the winner.
- Add the winner to the mating pool, which is initially empty.
- Repeat Steps 1-3 until the mating pool contains N_p individuals
- Stop

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Tournament selection : Example

$$N = 8, N_U = 2, N_p = 8$$

Input :

Individual Fintess

1	2	3	4	5	6	7	8
1.0	2.1	3.1	4.0	4.6	1.9	1.8	4.5

Output :

<u>Trial</u>	<u>Individuals</u>	Selected
1	2,4	4
2	3, 8	8
3	1, 3	3
4	4, 5	5
5	1,6	6
6	1, 2	2
7	4, 2	4
8	8, 3	8

If the fitness values of two individuals are same, than there is a tie in the match!! So, what to do????

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Note :

There are different twists can be made into the basic Tournament selection scheme:

- Frequency of N_U = small value (2,3), moderate 50 % of N and large $N_U \approx N$.
- Once an individual is selected for a mating pool, it can be discarded from the current population, thus disallowing the repetition in selecting an individual more than once.
- Replace the worst individual in the mating pool with those are not winners in any trials.

Steps :

- N_U individuals with highest fitness values are selected.
- 2 N_U individuals with worst fitness values are removed and N_U individuals selected in Step 1 are added into the mating pool.

This completes the selection procedure for one iteration. Repeat the iteration until the mating pool of desired size is obtained.

• Reference:

D. D. Goldberg and K. Deb, "A comparison of selection schemes in foundation of GA", Vol. 1, 1991, Pg. 69-93 Web link : K. Deb Website, IIT Kanpur

Elitisms

- In this scheme, an elite class (in terms of fitness) is identified first in a population of strings.
- It is then directly copied into the next generation to ensure their presence.



Comparing selection schemes

- Usually, a selection scheme follows Darwin's principle of "Survival of the fittest".
- In other words, a selection strategy in GA is a process that favours the selection of better individuals in the population for the matting pool (so that better genes are inherited to the new offspring) and hence search leads to the global optima.

There are two issues to decide the effectiveness of any selection scheme.

- Population diversity
- Selection pressure

Analyzing a selection schemes

More population diversity means more exploration

Higher selection pressure means lesser exploitation



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Population diversity

- This is similar to the concept of exploration.
- The population diversity means that the genes from the already discovered good individuals are exploited while permitting the new area of search space continue to be explored.

Selection pressure

- This is similar to the concept of exploitation.
- It is defined as the degree to which the better individuals are favoured.

Effectiveness of any selection schemes

These two factors are inversely related to each other in the sense that if the selection pressure increases, the population diversity decrease and vice-versa. Thus,

If selection pressure is HIGH

- The search focuses only on good individuals (in terms of fitness) at the moment.
- It loses the population diversity.
- Higher rate of convergence. Often leads to pre-mature convergence of the solution to a sub-optimal solution.

If the selection pressure is LOW

- May not be able to drive the search properly and consequently the stagnation may occurs.
- The convergence rate is low and GA takes unnecessary long time to find optimal solution.
- Accuracy of solution increases (as more genes are usually explored in the search).

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Soft Computing Applications

Analysis of different selection strategies

Selection Scheme	Population Diversity	Selection Pressure
Roulette-wheel selection	 Low Population Diversity 	 It is with high
	 Pre-mature convergence 	selection pressure
(It works fine when	 Less Accuracy in solution 	 Stagnation of Search
fitness values are		
informally distributed)		
Rank Selection	 Favors a high population diversity 	 Selection pressure is low
(It works fine when	- Slow rate of convergence	- Explore more
fitness values are not	0	solutions
necessarily uniformly		
distributed)		
Tournament Selection	 Population diversity is 	 It provides very high
	moderate	selection pressure
(It works fine when	- Ends up with a moderate	- better exploration of
population are with very	rate of convergence	search space
diversified fitness values)		
Steady-state Selection	 Population diversity is 	Selection pressure is
	decreases gradually as the	too low.
	generation advances	- Convergence rate is
		too slow
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The generation gap is defined as the proportion of individuals in the population, which are replaced in each generation, i.e

$$G_p = \frac{p}{N}$$

Where N is the population size and p is the number of individuals that will be replaced.

Note that in steady-state selection p = 2 and hence $G_p \approx 0$ for a large population whereas other selection schemes has $G_p \approx 1$

To make the G_p a large value, several strategies may be adopted.

- Selection of individuals according to their fitness and replacement at random
- Selection of individuals at random and replacement according to the inverse of their fitness values.
- Selection of both parents and replacement of according to fitness or inverse fitness.

Any question??

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